

# Compensation of Space-Charge Effects by "*Electron Columns*"

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# Space Charge Forces & Compensation

$$\xi_{SC} = \frac{B_f r_p N_{tot}}{4\pi\epsilon_n \beta \gamma^2}$$

Z, beam  
direction

$$\mathbf{B} = \beta \mathbf{E}$$

**Net force**

$$\mathbf{E} - \beta \mathbf{B} = \mathbf{E} / \gamma^2$$

protons

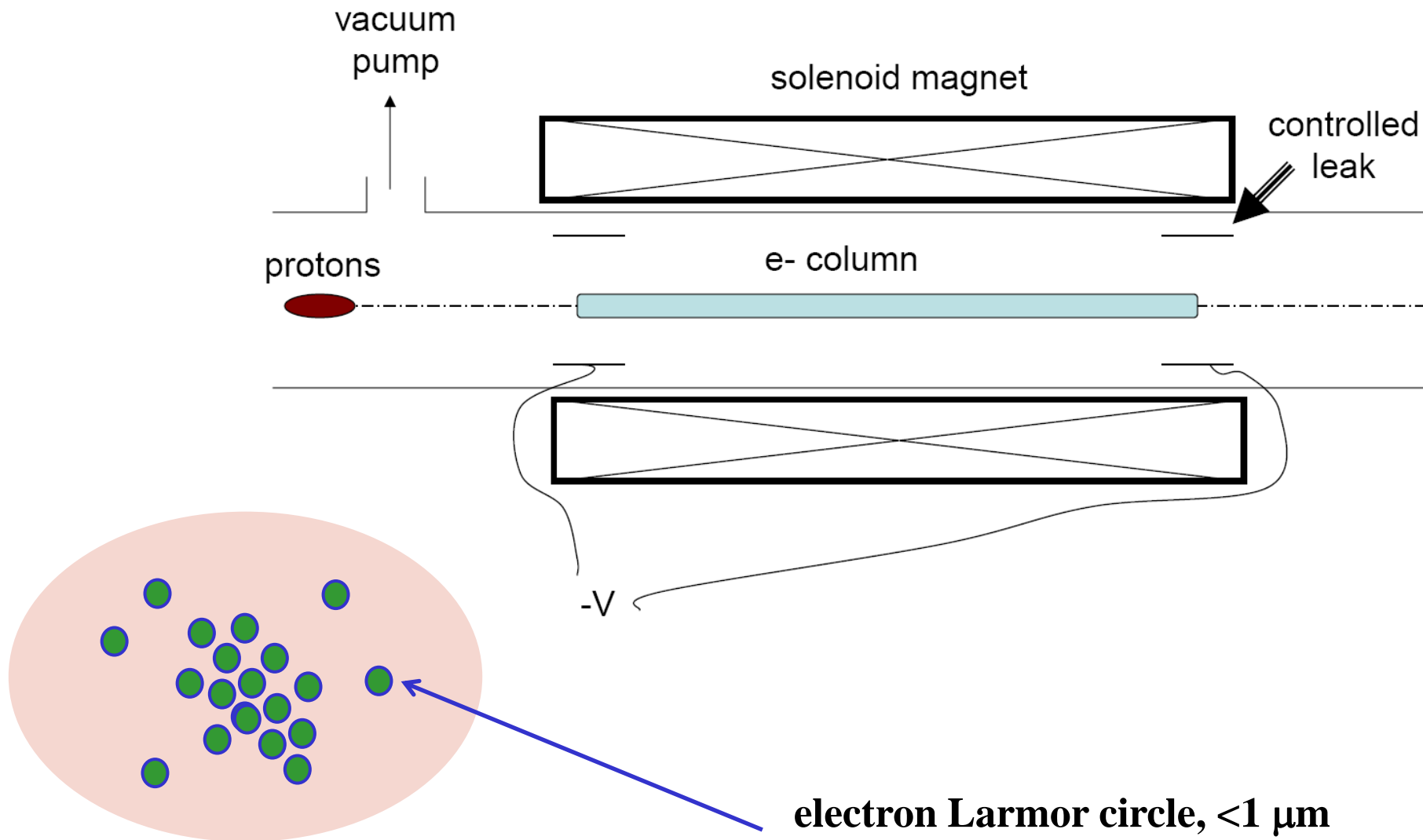
r, across the beam



1. Stability of the system (transverse motion)
  2. (Dynamic) matching of transverse p-charge distribution
  3. Appropriate longitudinal compensation (for not-flat proton bunches)
- Some indications of success with few MeV protons and e- from injected gas (Novosibirsk, 1970's)
  - The protons-electron system is **VERY** unstable
    - Now we know it as "electron cloud" effect
    - Vacuum worsening, beam instability, emittance growth
  - E-lenses proposed in 2000 - difficulty with #2
  - New idea which addresses #1, #2 and even #3 →

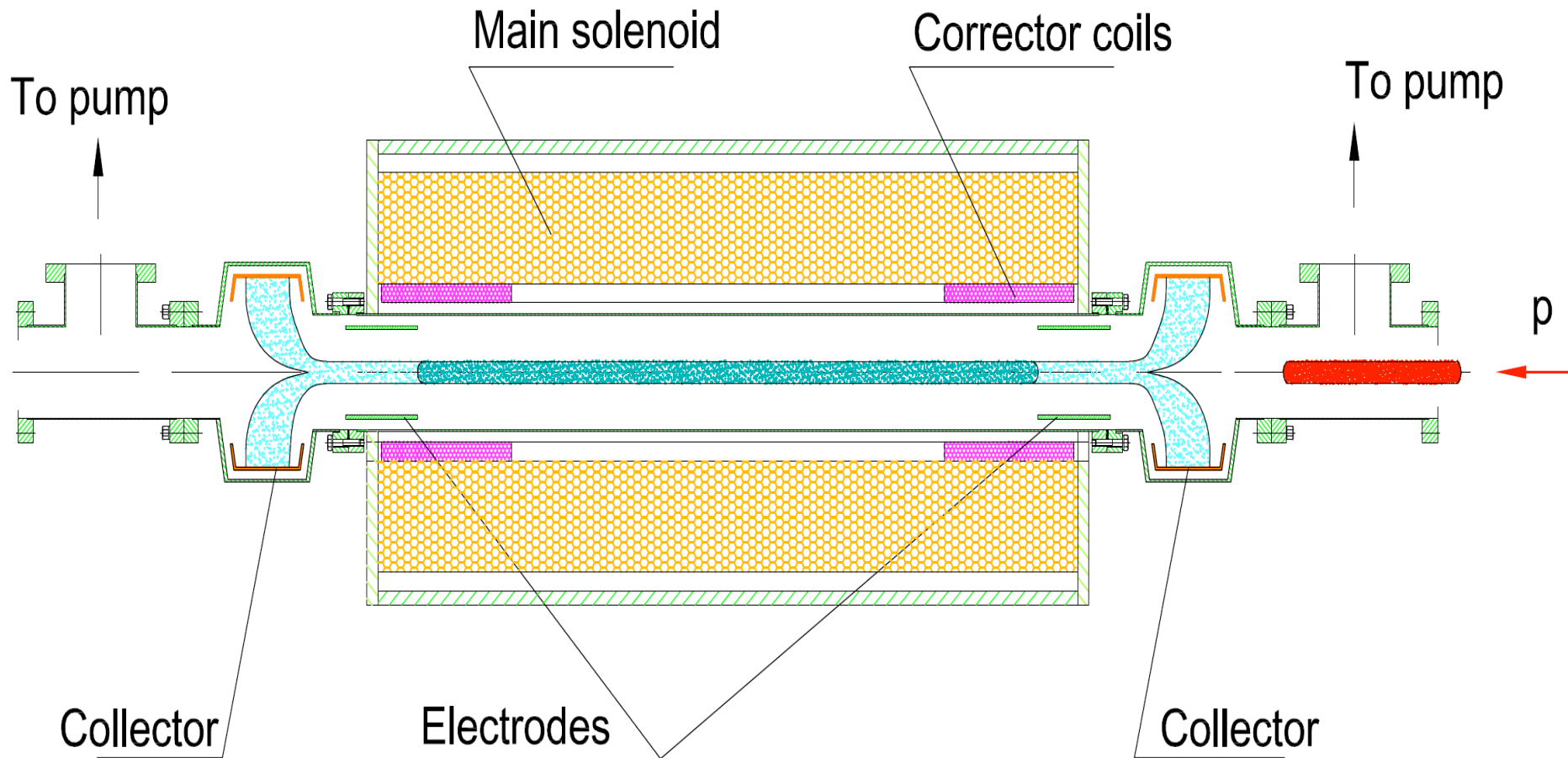


# Electron Column



electron Larmor circle,  $< 1 \mu\text{m}$

# E-Column in reality



- Instead of uniformly distributing electrons around the ring with low concentration :

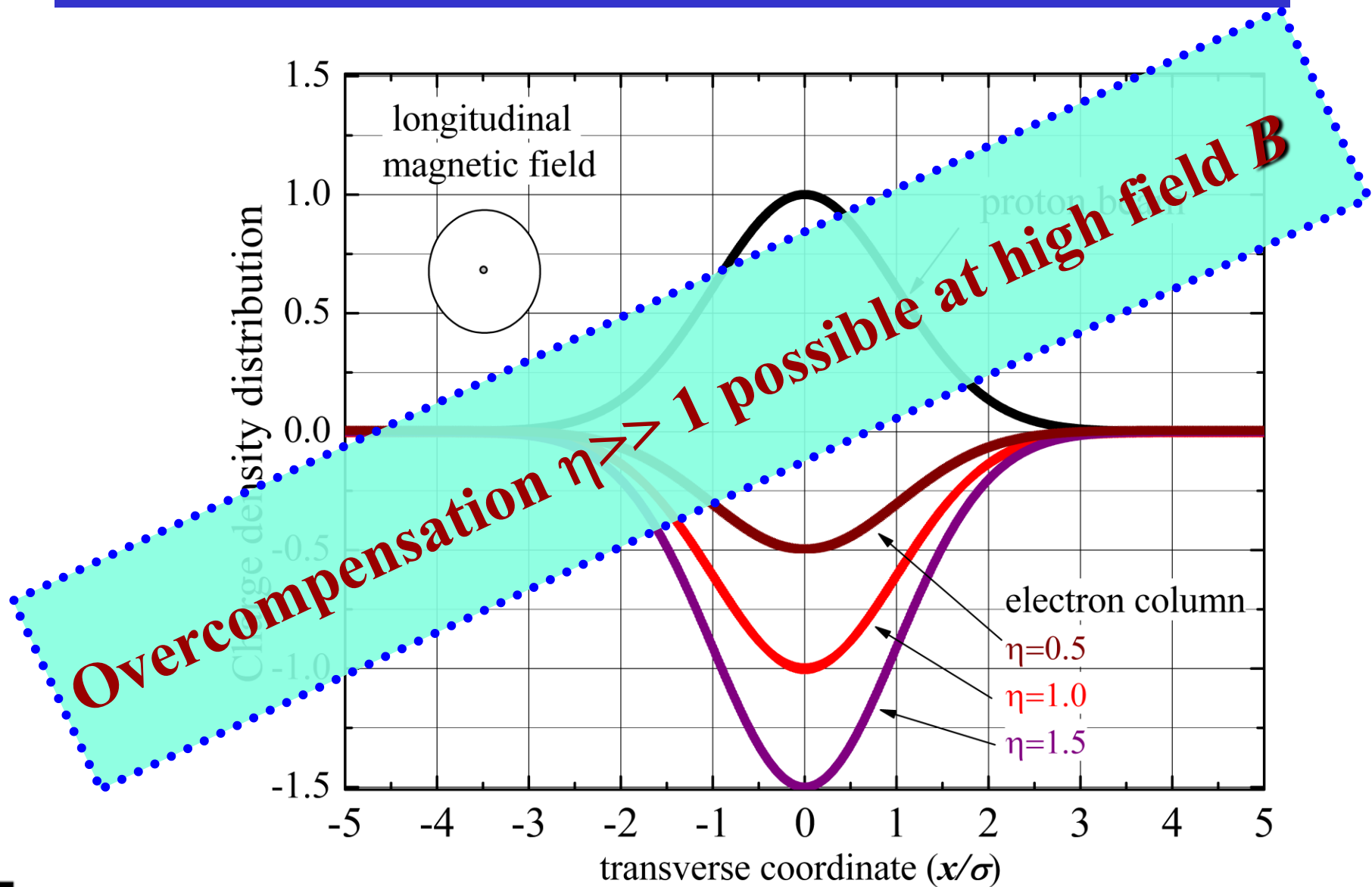
$$\eta = \frac{n_e}{n_p} = \frac{1}{\gamma^2}$$

- Electron columns will generate HIGH concentration of electrons but over a small fraction of ring circumference:

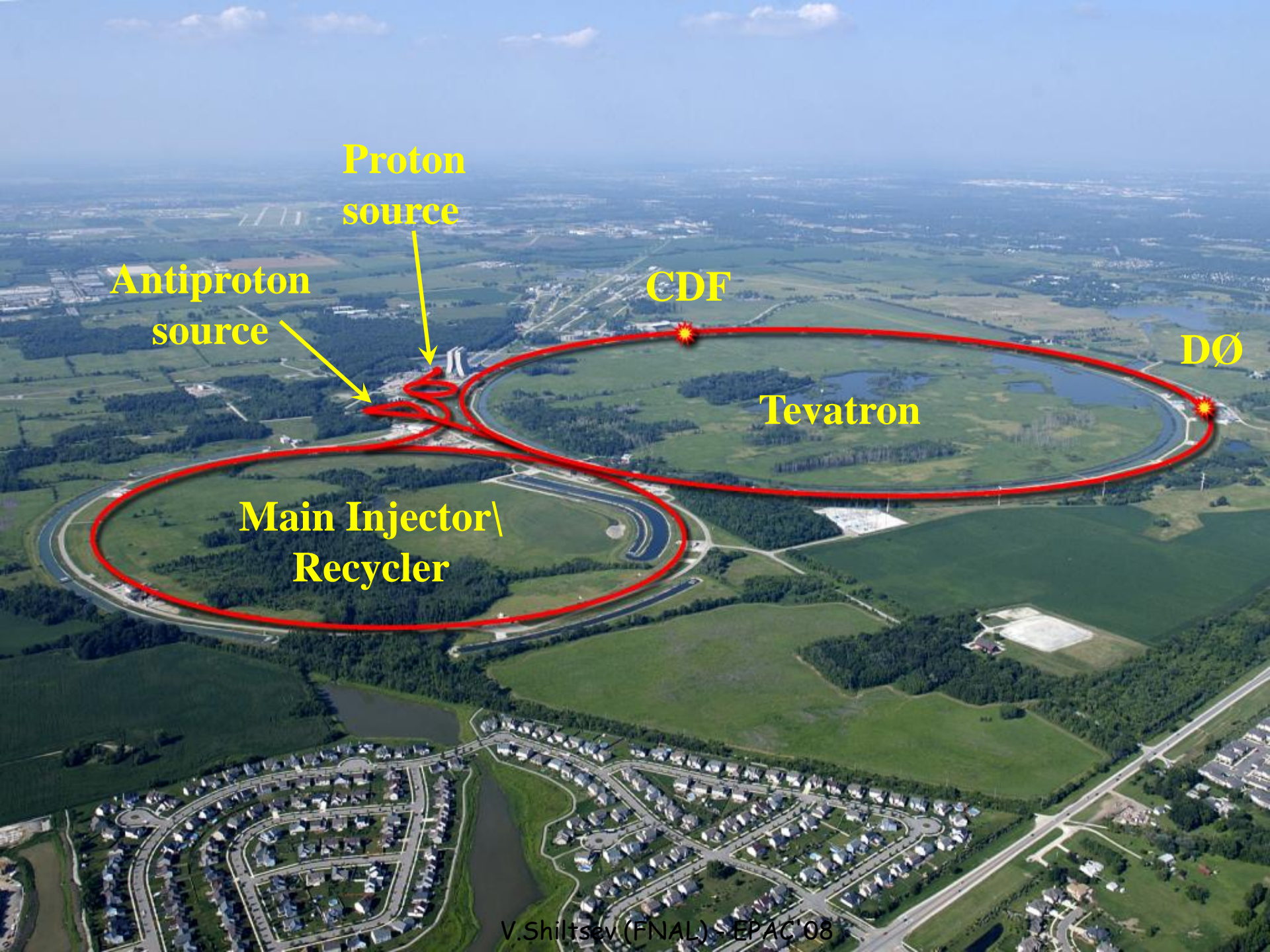
$$f = \frac{N_{EC} L_{EC}}{C} = \frac{\eta}{\gamma^2}$$



# How high local $\eta$ could be?







**Proton  
source**

**Antiproton  
source**

**CDF**

**DØ**

**Tevatron**

**Main Injector\  
Recycler**



# Some Examples

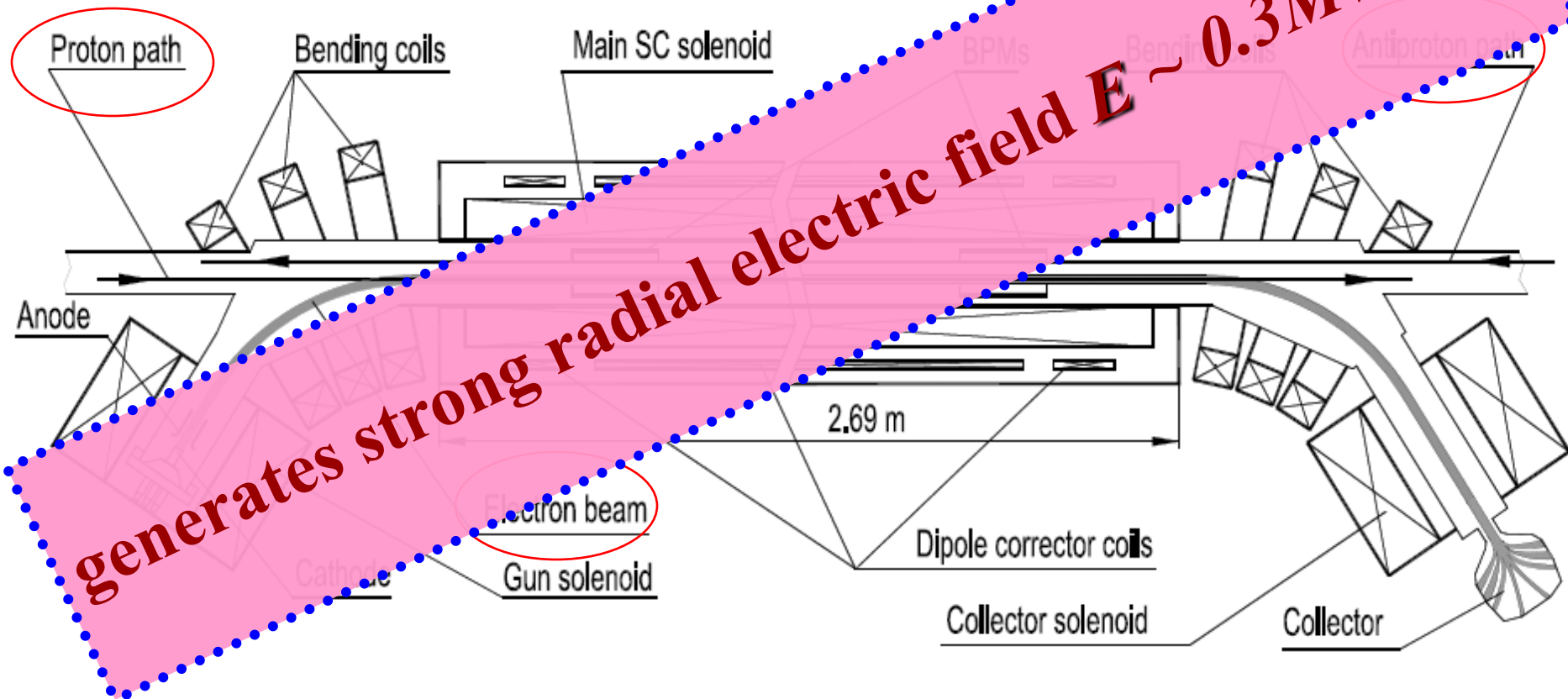
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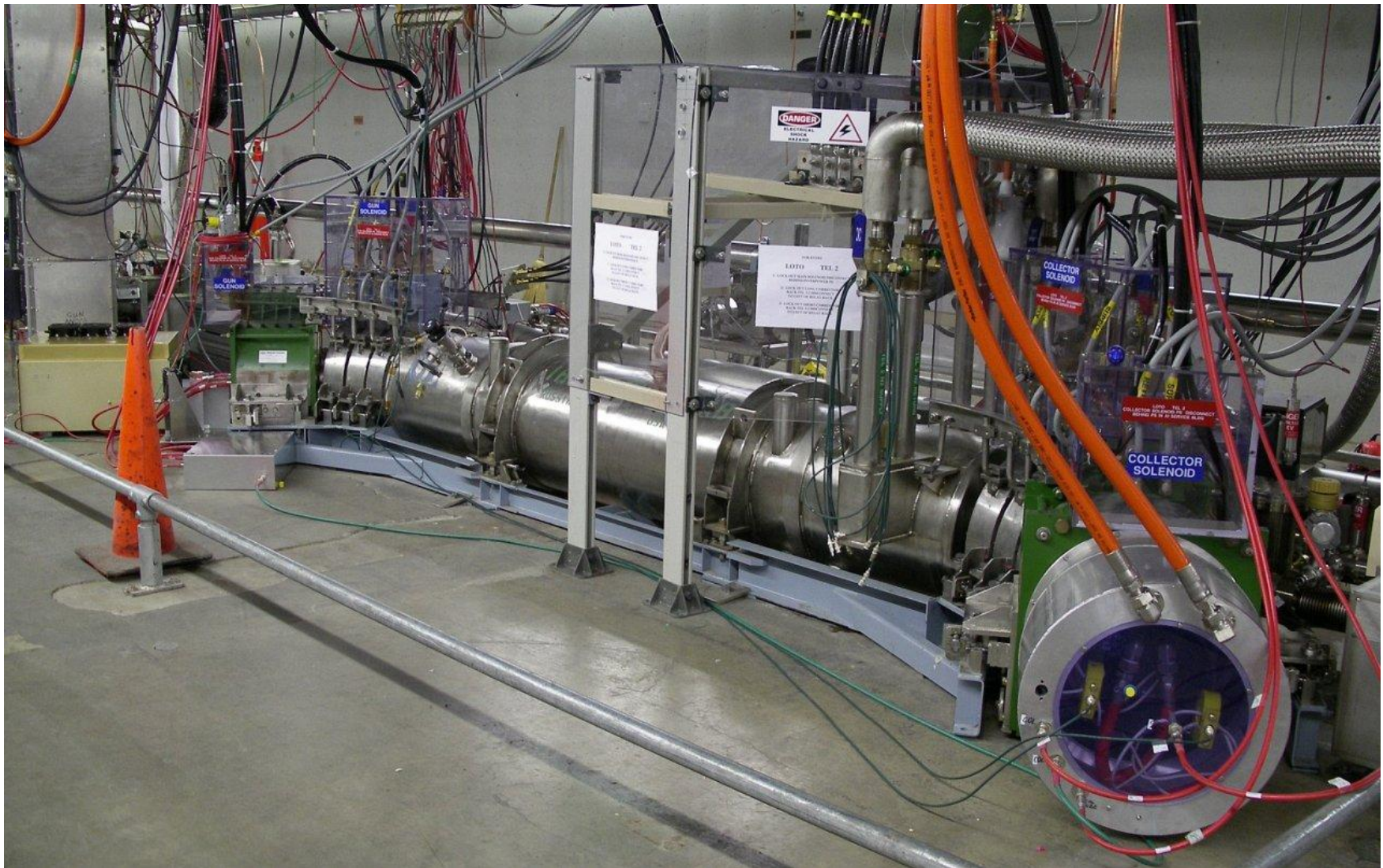
	$C$ [km]	$E$ [GeV]	$\xi_{SC}$	$N_{EC}L_{EC}$
Booster	0.48	0.4	$\sim 0.3$	$\sim 120m$
Main Injector	3.3	8.0	0.06+	$\sim 20m$
Recycler	3.3	8.0	0.12+	$\sim 40m$



# Compare with Electron Lens

~4 mm dia 2 m long very straight beam of ~10 kV  
~1 A electrons ( $\sim 10^{12}$ ) immersed in





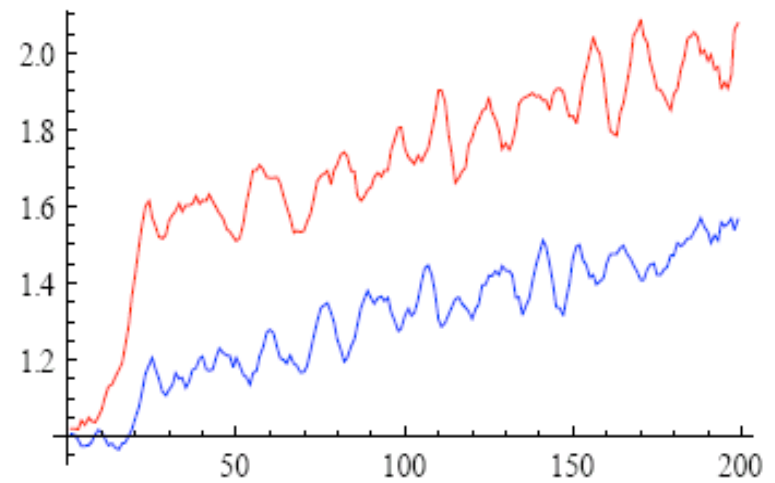
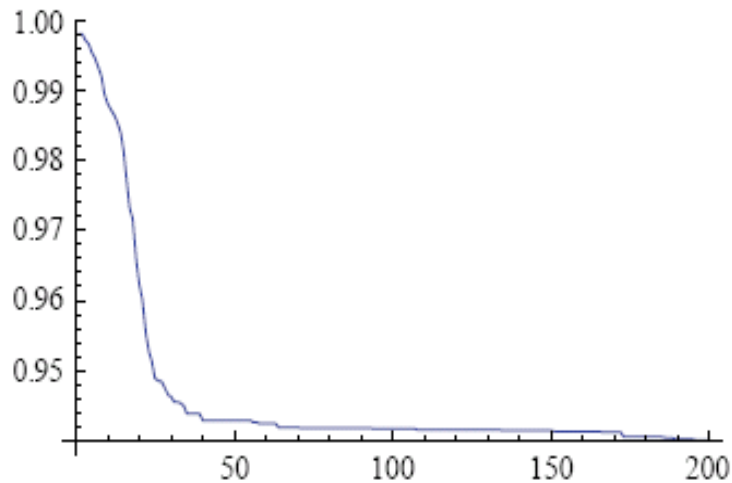


*Yu.Alexahin*  
*V.Kapin*

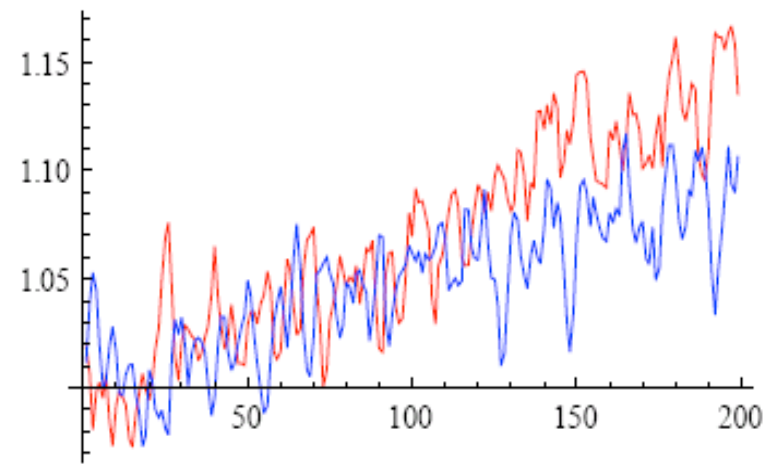
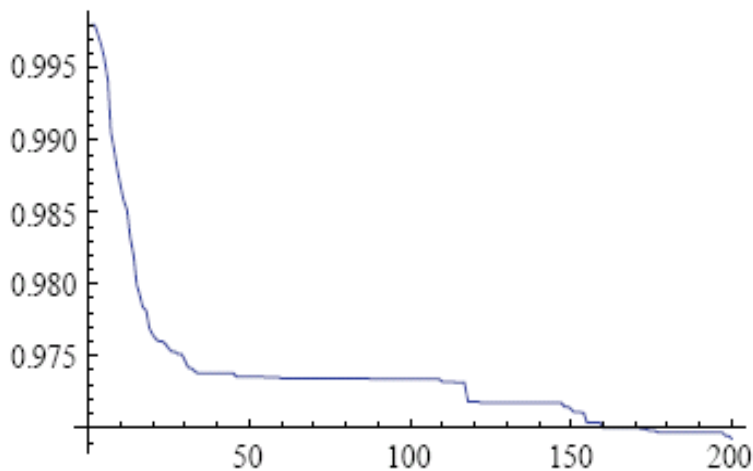
$N/N_0$

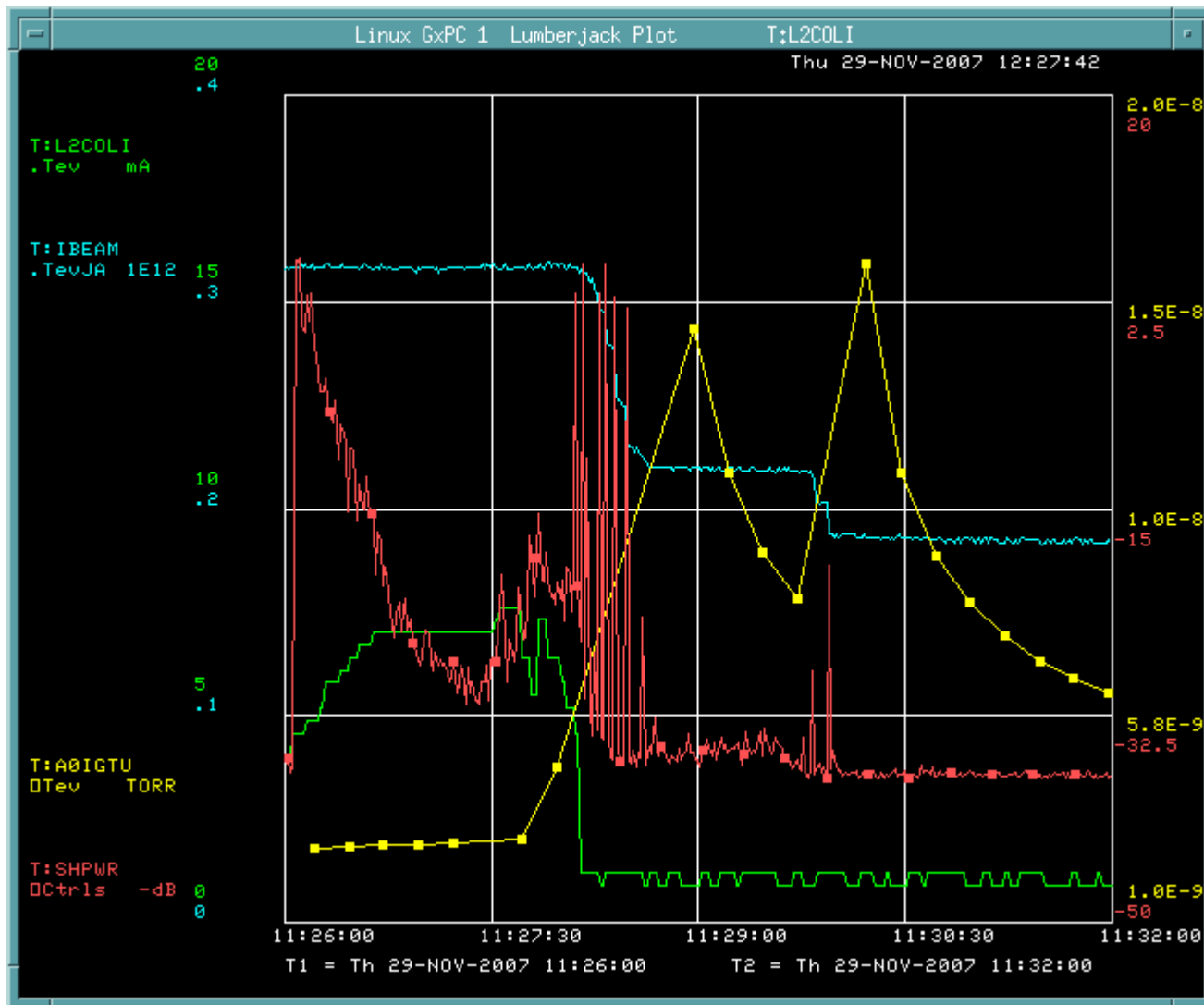
$\epsilon_x/\epsilon_0, \epsilon_y/\epsilon_0$

$f=0$



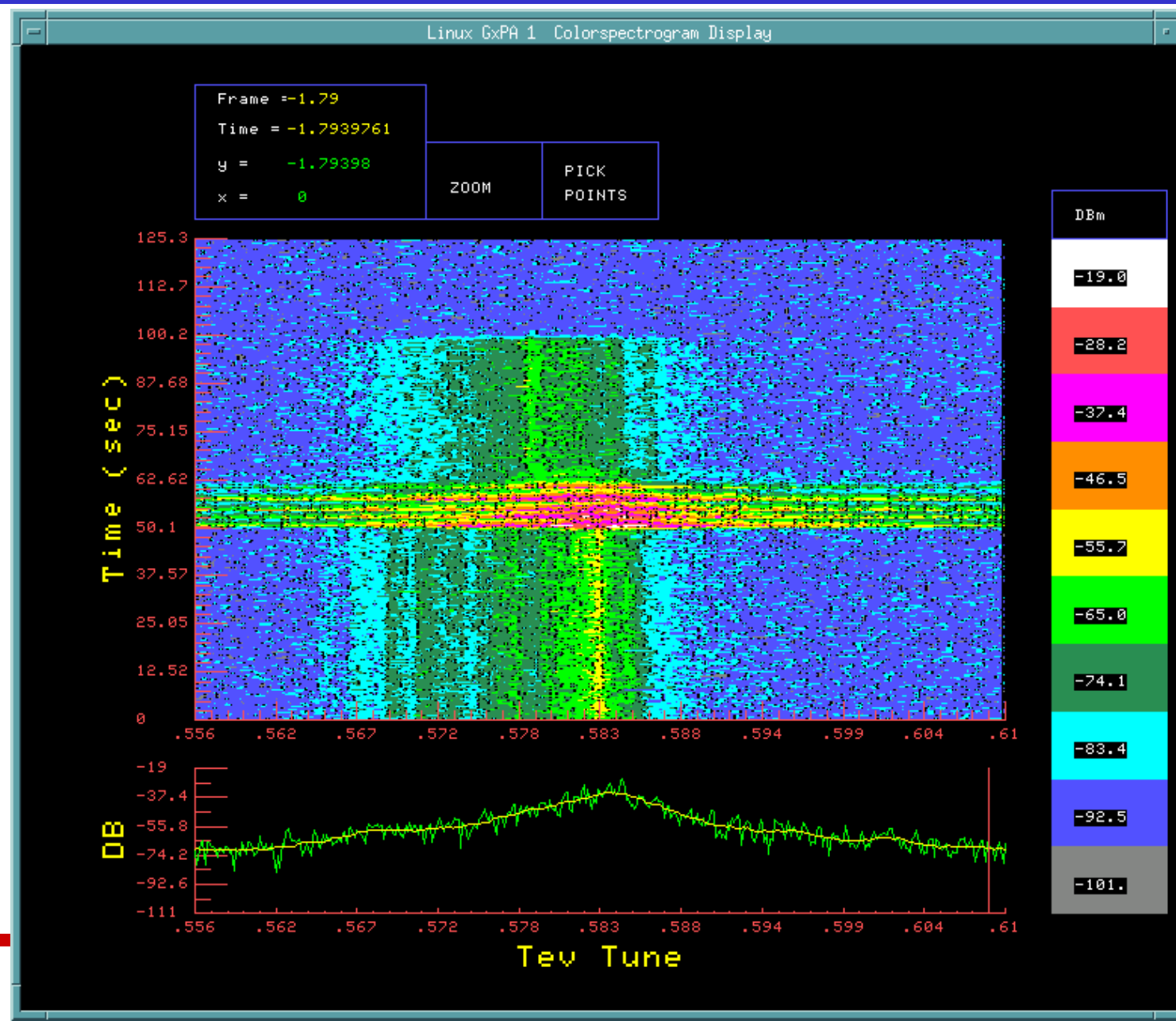
$f=0.5$





**emittance ratio ( $\epsilon_p/\epsilon_a$ )  $\sim 3$**





- Further tests in the Tevatron to be performed with better vacuum control ( $1e-7$ , no e-beam help)
- **Simulation and analysis to address:**
  - Maximum B-field needed for high  $\eta$
  - Tolerances on profile matching
  - How many (few) e-columns needed in SuperPeriod=1 machines like Main Injector and Recycler
  - ExB e-dynamics if proton beam x,y sizes are not equal
- ...if successful- Build a (cheap) e-Column prototype for studies in MI
- ... if successful - Build and install as many as needed for Space-Charge Compensation in MI and RR operation during *Project-X* era





*That's All, Folks!*

# Back-up slides

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$$\tau_n = \frac{1}{\sigma_{\text{ioniz}} \cdot v_p \cdot n_0}$$

$$\tau_n \approx \frac{0.05 \text{ ns}}{P [\text{Torr}]}$$

$$\sigma_{\text{ioniz}} \approx 2 \cdot 10^{-17} \text{ cm}^2$$

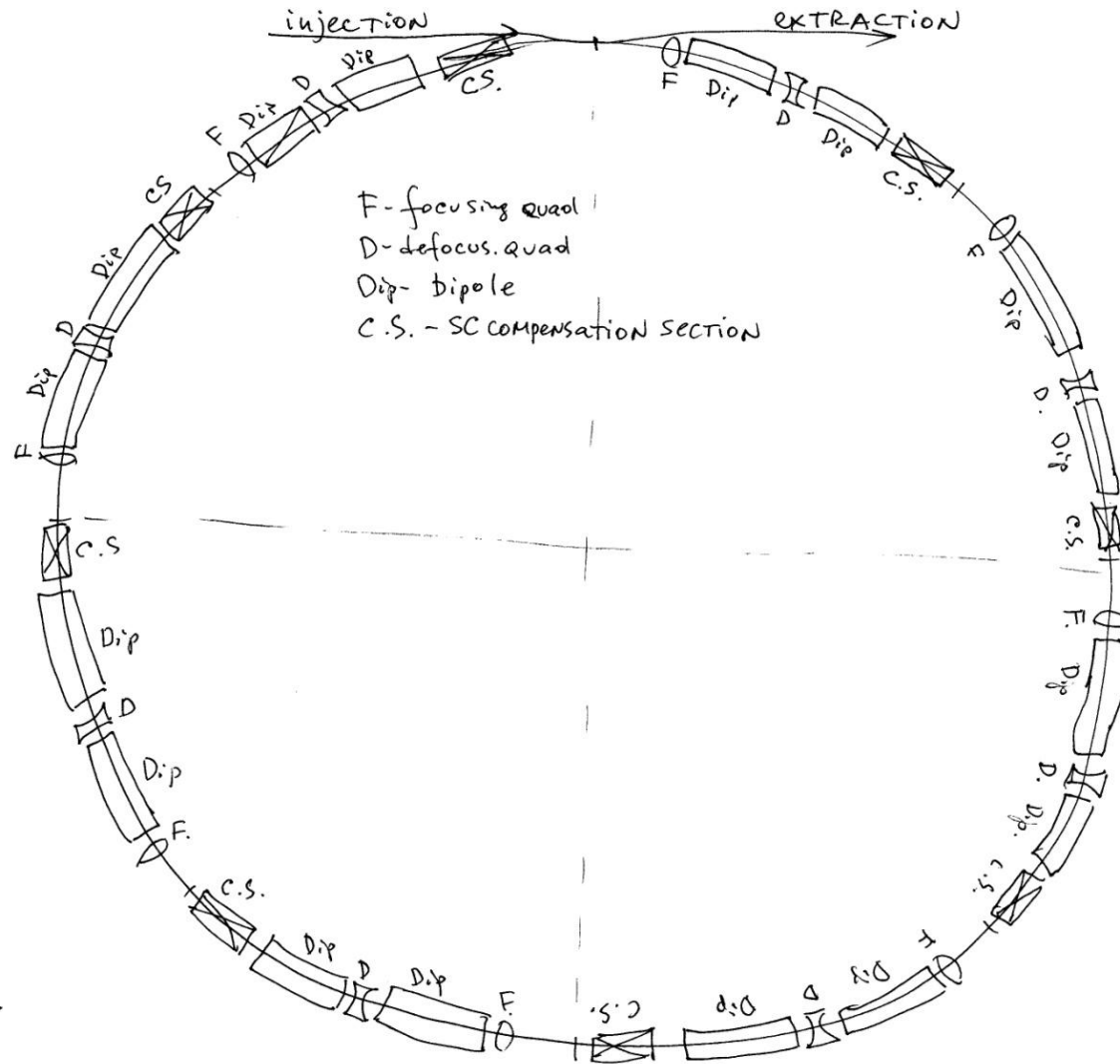
$$n_0 = \frac{2.5 \cdot 10^{-10}}{P [\text{Torr}]} \text{ cm}^{-3}$$

$$v_p \approx c$$





# Ideal ring with e-columns



# Possible Solenoid Configurations

